# Cohomological Subsectors in Sigma Models on Superspaces

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Motivation Observation

Calculation of some correlators in the  $\sigma$ -models on the l.h.s where mapped onto the correlators of the free theories on the r.h.s.:

$\sigma$ -model	subsector
$S^{3 2} = \frac{\operatorname{OSp}(4 2)}{\operatorname{OSp}(3 2)}$	<i>S</i> <sup>1</sup> or free compact boson [CC, Saleur, 08], [Mitev, Quela, Schomerus 08]
$\mathbb{C}P^{1 2} = \frac{\mathrm{U}(2 2)}{\mathrm{U}(1) \times \mathrm{U}(1 2)}$	$\mathbb{C}P^{0 1}$ or free symplectic fermions [CC, Read, Jacobsen Saleur 09], [CC, Mitev, Quella, Saleur, Schomerus 09]

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• How to characterize the set of fields in the  $S^{3|2}$  and  $\mathbb{C}P^{1|2} \sigma$ -models whose correlators can be computed within the simpler theories?

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- How to characterize the set of fields in the  $S^{3|2}$  and  $\mathbb{C}P^{1|2} \sigma$ -models whose correlators can be computed within the simpler theories?
- What is the exact connexion between the full theory and the subsector theory? Both field theories being  $\sigma$ -models, there must be a geometric construction connecting them.

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- What is the exact connexion between the full theory and the subsector theory? Both field theories being  $\sigma$ -models, there must be a geometric construction connecting them.
- How much of the structure (conformal invariance, integrability) of the subsector theory lifts to the full theory?

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- How to characterize the set of fields in the  $S^{3|2}$  and  $\mathbb{C}P^{1|2} \sigma$ -models whose correlators can be computed within the simpler theories?
- What is the exact connexion between the full theory and the subsector theory? Both field theories being  $\sigma$ -models, there must be a geometric construction connecting them.
- How much of the structure (conformal invariance, integrability) of the subsector theory lifts to the full theory?
- Is the existence of simplified subsectors a general feature of  $\sigma$ -models on G/G' superspaces? If yes, then are the simplified subsectors equivalent again to  $\sigma$ -models on H/H' superspace?

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Target space cohomology

# Finding the right approach Spin chains

$$\begin{aligned} \operatorname{OSp}(2N+2|2N) \operatorname{chain} V_{2N+2|2N}^{\otimes L} & \operatorname{GL}(N|N) \operatorname{chain} (V_{N|N} \otimes V^*_{N|N})^{\otimes L} \\ H_N^{\operatorname{OSp}} &= \operatorname{rep}_N(H_{\operatorname{Brauer}}) & H_N^{\operatorname{GL}} &= \operatorname{rep}_N(H_{\operatorname{Brauer}}^{\operatorname{walled}}) \\ H_{\operatorname{Brauer}} &= \sum E_{i,i+1} + wP_{i,i+1} & H_{\operatorname{Brauer}}^{\operatorname{walled}} &= \sum E_{i,i+1} + wP_{i,i+2} \\ \operatorname{have been extensively studied as discretizations of boundary } \sigma \operatorname{-models} \\ S^{2N+1|2N} &= \frac{\operatorname{OSp}(2N+2|2N)}{\operatorname{OSp}(2N+1|2N)} & \mathbb{C}P^{N-1|N} &= \frac{\operatorname{U}(N|N)}{\operatorname{U}(1) \times \operatorname{U}(N-1|N)} \\ \operatorname{[CC, Saleur 08]} & \mathbb{C}P^{N-1|N} &= \frac{\operatorname{U}(N|N)}{\operatorname{U}(1) \times \operatorname{U}(N-1|N)} \end{aligned}$$

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Embedding of spectra spec  $H_0 \subset \operatorname{spec} H_1 \subset \cdots \subset \operatorname{spec} H^{(walled)}_{\operatorname{Brauer}}$ 

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$$OSp(2N + 2|2N) \operatorname{chain} V_{2N+2|2N}^{\otimes L} \qquad GL(N|N) \operatorname{chain} (V_{N|N} \otimes V_{N|N}^*)^{\otimes L}$$

$$H_N^{OSp} = \operatorname{rep}_N(H_{Brauer}) \qquad H_N^{GL} = \operatorname{rep}_N(H_{Brauer}^{\otimes led}) \qquad H_N^{GL} = \operatorname{rep}_N(H_{Brauer}^{\otimes led}) \qquad H_N^{\otimes led} = \sum E_{i,i+1} + wP_{i,i+2} \qquad H_{Brauer}^{\otimes led} = \sum E_{i,i+1} + wP_{i,i+2} \qquad H_{Braue}^{\otimes led} = \sum$$

Reduction of  $\sigma$ -models on G/G' superspaces

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## Mathematical definitions and constructions Lie superalgebras

### Cohomological reduction of a Lie superalgebra g

with respect to an odd element Q, such that  $[Q, Q] = 2Q^2 = 0$ , is the Lie superalgebra defined as

$$\mathsf{H}_{\mathcal{Q}}(\mathfrak{g}) = \frac{\mathsf{Ker}[\mathcal{Q}, \cdot]}{\mathsf{Im}[\mathcal{Q}, \cdot]} = \frac{\mathsf{Ker}_{\mathcal{Q}}\,\mathfrak{g}}{\mathsf{Im}_{\mathcal{Q}}\,\mathfrak{g}}$$

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 $r_O = \operatorname{rank}(Q)$ 

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## Classification of cohomological reductions

$$\begin{aligned} \mathsf{H}_{\mathcal{Q}}\left(\operatorname{gl}(M|N)\right) &\simeq \operatorname{gl}(M - r_{\mathcal{Q}}|N - r_{\mathcal{Q}}) \\ \mathsf{H}_{\mathcal{Q}}\left(\operatorname{sl}(M|N)\right) &\simeq \operatorname{sl}(M - r_{\mathcal{Q}}|N - r_{\mathcal{Q}}) \\ \mathsf{H}_{\mathcal{Q}}\left(\operatorname{osp}(M|2N)\right) &\simeq \operatorname{osp}(M - 2r_{\mathcal{Q}}|2N - 2r_{\mathcal{Q}}) \end{aligned}$$

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## Mathematical definitions and constructions Modules

Cohomological reduction of a  $\mathfrak{g}$ -module V is the  $\mathsf{H}_Q(\mathfrak{g})$ -module defined as

$$\mathsf{H}_{\mathcal{Q}}(V) = \frac{\operatorname{\mathsf{Ker}} Q : V \mapsto V}{\operatorname{\mathsf{Im}} Q : V \mapsto V} = \frac{\operatorname{\mathsf{Ker}}_{\mathcal{Q}} V}{\operatorname{\mathsf{Im}}_{\mathcal{Q}} V}$$



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## Properties

• if  $V \simeq V^*$  then

$$V|_{\mathsf{H}_{\mathcal{Q}}(\mathfrak{g})} \simeq W \oplus E \oplus F$$
$$W \simeq \mathsf{H}_{\mathcal{Q}}(V), E = \mathsf{Im}_{\mathcal{Q}} V$$

- $\mathsf{H}_{\mathcal{Q}}(U \oplus V) \simeq \mathsf{H}_{\mathcal{Q}}(U) \oplus \mathsf{H}_{\mathcal{Q}}(V)$
- $\mathsf{H}_Q(U^*) \simeq \left(\mathsf{H}_Q(U)\right)^*$
- $\mathsf{H}_{\mathcal{Q}}(U \otimes V) \simeq \mathsf{H}_{\mathcal{Q}}(U) \otimes \mathsf{H}_{\mathcal{Q}}(V)$

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•  $\operatorname{sdim} \operatorname{H}_Q(V) = \operatorname{sdim} V$ 

## Mathematical definitions and constructions Modules

Cohomological reduction of a g-module V is the  $H_O(g)$ -module defined as

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## Properties

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$$W \simeq \mathsf{H}_{\mathcal{Q}}(V), E = \mathsf{Im}_{\mathcal{Q}} V$$

- $H_{O}(U \oplus V) \simeq H_{O}(U) \oplus H_{O}(V)$
- $\mathsf{H}_{\mathcal{O}}(U^*) \simeq \left(\mathsf{H}_{\mathcal{O}}(U)\right)^*$
- $\mathsf{H}_{\mathcal{O}}(U \otimes V) \simeq \mathsf{H}_{\mathcal{O}}(U) \otimes \mathsf{H}_{\mathcal{O}}(V)$
- sdim  $H_Q(V) = sdim V$

- $\mathsf{H}_{O}(V_{2N+2|2N}) \simeq V_{2n+2|2n}$
- $\mathsf{H}_{O}(V_{2N+2|2N})^{\otimes L} \simeq (V_{2n+2|2n})^{\otimes L}$

Reduction of  $\sigma$ -models on G/G' superspaces

•  $\mathsf{H}_O(V_{N|N}) \simeq V_{n|n}$ 

• 
$$\mathsf{H}_Q(V_{N|N}) \overset{\otimes L}{\underset{\square}{\otimes}} \simeq (V_{n|n}) \overset{\otimes L}{\underset{\square}{\otimes}}$$

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 $n=N-r_0$ 

## Cohomological reduction of sigma models Target space cohomology

## Set-up

- Pick target space supersymmetry Q,  $Q^2 = 0$ . Correlation functions of Q-invariant local fields depend only on their Q-cohomology.
- Compute the *Q*-cohomology of the space of local fields. Interpret the result as the space of local fields of a reduced field theory.
- Map the correlators of *Q*-invariant local fields to correlators in the reduced theory.

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Map the correlators of *Q*-invariant local fields to correlators in the reduced theory.

# Cohomological reduction as a geometrical problem

geometrical object

- $T(G/G')^{\otimes n} \otimes L_2(G/G')$
- *G*-invariant symm/antisymm form of rank 2

field theory object

• *n*-worldsheet derivative fields

• kinetic/*B*-field or  $\theta$ -terms in the action

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# Target space cohomology Notations

# Define the superalgebras

$$Q\in\mathfrak{g}'\subset\mathfrak{g}$$

$$\begin{split} \mathfrak{g}' &\simeq \mathfrak{h}' \oplus \mathfrak{e}' \oplus \mathfrak{f}' & \subset & \mathfrak{g} \simeq \mathfrak{h} \oplus \mathfrak{e} \oplus \mathfrak{f} \\ \mathfrak{h}' &\simeq \mathsf{H}_Q(\mathfrak{g}') & \subset & \mathfrak{h} \simeq \mathsf{H}_Q(\mathfrak{g}) \\ \mathfrak{e}' &= \mathsf{Im}_Q \,\mathfrak{g}' & \subset & \mathfrak{e} &= \mathsf{Im}_Q \,\mathfrak{g} \end{split}$$

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# Target space cohomology Notations

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$\mathfrak{g}'\simeq\mathfrak{h}'\oplus\mathfrak{e}'\oplus\mathfrak{f}'$	$\subset$	$\mathfrak{g}\simeq\mathfrak{h}\oplus\mathfrak{e}\oplus\mathfrak{f}$
$\mathfrak{h}'\simeq H_\mathcal{Q}(\mathfrak{g}')$	$\subset$	$\mathfrak{h}\simeqH_{\mathcal{Q}}(\mathfrak{g})$
$\mathfrak{e}' = \operatorname{Im}_Q \mathfrak{g}'$	$\subset$	$\mathfrak{e} = Im_Q  \mathfrak{g}$

## Define the supergroups with corresponding Lie superalgebras

G'	$\subset$	G
U		U
H'	C	Н

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## Target space cohomology Notations

# Define the superalgebras



$$\begin{array}{ll} \mathfrak{g}' \simeq \mathfrak{h}' \oplus \mathfrak{e}' \oplus \mathfrak{f}' & \subset & \mathfrak{g} \simeq \mathfrak{h} \oplus \mathfrak{e} \oplus \mathfrak{f} \\ \mathfrak{h}' \simeq H_Q(\mathfrak{g}') & \subset & \mathfrak{h} \simeq H_Q(\mathfrak{g}) \\ \mathfrak{e}' = \operatorname{Im}_Q \mathfrak{g}' & \subset & \mathfrak{e} = \operatorname{Im}_Q \mathfrak{g} \end{array}$$

## Define the supergroups with corresponding Lie superalgebras

G'	$\subset$	G
U		U
H'	C	Н

Then one has

 $H/H'\subset G/G'$  .

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#### Target space cohomology Central results

# Cohomology evaluation

$$\mathsf{H}_Q\left(T^{\otimes n}(G/G') \otimes L_2(G/G')
ight)$$

Q-invariant tensor form  $\omega$  of

rank *n* on G/G'

 $\omega$ 

 $\simeq T^{\otimes n}(H/H') \otimes L_2(H/H')$   $\stackrel{\rho}{\mapsto} \rho(\omega)$ restriction  $\rho(\omega)$  of  $\omega$  to  $\bullet \text{ submanifold } H/H' \subset G/G'$   $\bullet T^{\otimes n}(H/H') \subset T^{\otimes n}(G/G')|_{H/H'}$ 

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#### Target space cohomology Central results

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• 
$$T^{\otimes n}(H/H') \subset T^{\otimes n}(G/G')|_{H/H'}$$

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## Localization formula

rank *n* on G/G'

Q-invariant tensor form  $\omega$  of

$$\int_{G/G'} \omega = \int_{H/H'} \rho(\omega)$$

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# Cohomological reduction of $\sigma$ -models Results

## Space of local fields

*Q*-cohomology of the space of local fields in the  $\sigma$ -model on G/G' identified with the space of local fields in the  $\sigma$ -model on H/H'.

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*Q*-cohomology of the space of local fields in the  $\sigma$ -model on G/G' identified with the space of local fields in the  $\sigma$ -model on H/H'.

## Action

Restriction of a G-invariant metric/2-form on G/G' to

- the points of  $H/H' \subset G/G'$
- the tensor space  $T^{\otimes 2}(H/H') \subset T^{\otimes 2}(G/G')|_{H/H'}$

$$S_{H/H'} = \rho(S_{G/G'})$$

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obviously gives an *H*-invariant metric/2-form on H/H'

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obviously gives an H-invariant metric/2-form on H/H'

## Correlation functions

$$\left\langle \prod_{i} O(x_i) \right\rangle_{G/G'} = \left\langle \prod_{i} \rho(O_i)(x_i) \right\rangle_{H/H'}$$

Reduction of  $\sigma$ -models on G/G' superspaces

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CFT  $\sigma$ -models on symmetric superspaces Applications of cohomological reductions

## reduced model H/H' conformal invariant

- G/G' admits a single radius only
- $c_{H/H'} \neq 0$

 $\sigma$ -model G/G' is conformal invariant

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CFT  $\sigma$ -models on symmetric superspaces Applications of cohomological reductions

reduced model H/H' conformal invariant

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 $\Rightarrow \quad \begin{array}{l} \sigma \text{-model } G/G' \text{ is} \\ \text{ conformal invariant} \end{array}$ 

Classification of CFT  $\sigma$ -models on G/G' superspaces with one radius only

$\sigma$ -model	maximal reduction		
$\frac{OSp(2M+2N+2 2M+2N)}{OSp(2M+1 2M) \times OSp(2N+1 2N)}$	free		
OSp(2N+2 2N)	compact		
D(2,1;lpha)	boson		
$\frac{\operatorname{GL}(M+N+1 M+N+1)}{\operatorname{GL}(M+1 N)\times\operatorname{GL}(M N+1)}$	free		
$\frac{\mathrm{PSL}(2N 2N)}{\mathrm{OSp}(2N 2N)}$	symplectic		
PSL(N N)	fermions		
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Reduction of $\sigma$ -models on $G/G'$ superspaces	C. Candu 🛞		12/1

• WZW  $\sigma$ -models can be reduced with the same tools: restriction of a *G*-invariant 3-form on *G* is again an *H*-invariant 3-form on *H*.

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- OSp(M|2N) Landau-Ginsburg

$$S = \int d^2x \left[ (\partial_\mu \Phi, \partial_\mu \Phi) + g(\Phi, \Phi)^2 
ight] \, ,$$

where  $\Phi$  is an even field in the fundamental representation,

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$$S = \int d^2 x \left[ (\partial_\mu \Phi, \partial_\mu \Phi) + g(\Phi, \Phi)^2 
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where  $\Phi$  is an even field in the fundamental representation, and Gross-Neveu models

$$S = \int d^2x \left[ (\Psi, \bar{\partial}\Psi) + (\bar{\Psi}, \partial\bar{\Psi}) + g(\Psi, \bar{\Psi})^2 
ight],$$

where  $\Psi, \bar{\Psi}$  are an odd fields in the fundamental representation, can be reduced to corresponding  $OSp(M - 2r_Q|N - 2r_Q)$  models.

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• Spin chains.

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#### Conclusions

### Results

- Mapping of *Q*-invariant correlation functions of local fields in the G/G' $\sigma$ -model to correlation functions in an  $H/H' \sigma$ -model.
- Classification of CFT  $\sigma$ -models with one radius.
- Extension of cohomological reduction to WZW, Landau-Ginsburg and Gross-Neveu models. Main idea applicable even to spin chains.

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## Outlook

- Reduction with respect to a target space supersymmetry *Q* that does not belong to the Lie superalgebra of the denominator group.
- Extension to string theory in the pure spinor formalism. Proof of conformal invariance.
- How does the integrability of a cohomological subsector constraint the integrability of the full theory?

